

## **Cambridge International Examinations**

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME						
CENTRE NUMBER		CANDIDATE NUMBER				
MATHEMATICS			0580/42			
Paper 4 (Extended)		October/November 2015				
		2	hours 30 minutes			
Candidates answer or	n the Question Paper.					
Additional Materials:	Electronic calculator Tracing paper (optional)	Geometrical instruments				

## **READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total of the marks for this paper is 130.

The syllabus is approved for use in England, Wales and Northern Ireland as a Cambridge International Level 1/Level 2 Certificate.

CAMBRIDGE
International Examinations

		ompany uses 512 actors in a film.  rs are in the ratio men: women: children = 7: 11: 14.
(a)	(i)	Show that there are 224 children in the film.
		Answer(a)(i)
		[2]
	(ii)	Find the number of men in the film.
		Answer(a)(ii)[1]
(b)		ry working day, each child is given \$1 to spend. h child works for 45 days.
		culate the total amount that the film company gives the children to spend. e your answer correct to the nearest \$100.
		Answer(b) \$[2]
(c)		children have lessons every day in groups of no more than 12.
	Calo	culate the smallest possible number of groups.
		Answer(c)[2]
(d)	The	film costs four million and ninety three thousand dollars to make.
	(i)	Write this number in figures.
		<i>Answer(d)</i> (i)[1]
	(ii)	Write your answer to part (d)(i) in standard form.
		Answer(d)(ii)[1]
(e)		VD copy of the film costs \$2.75 to make. selling price is \$8.20.
	Calo	culate the percentage profit.

Answer(e) ......% [3]

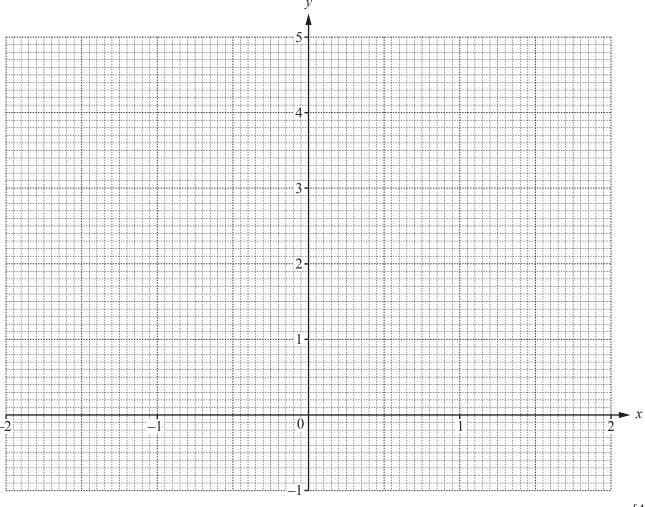
2 The table shows some values for  $y = x^3 - 3x + 2$ .

x	-2	-1.5	-1	-0.5	0	0.5	1	1.5	2
у		3.125		3.375	2		0		4

(a) Complete the table of values.

[4]

**(b)** On the grid, draw the graph of  $y = x^3 - 3x + 2$  for  $-2 \le x \le 2$ .



[4]

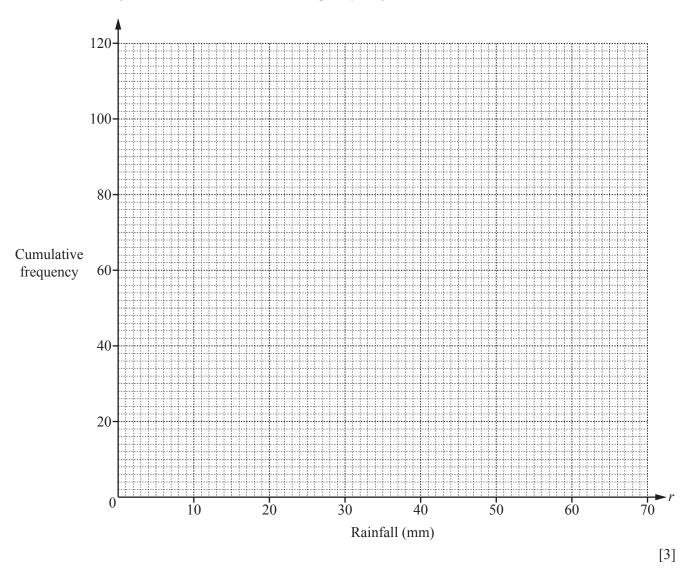
(c) By drawing a suitable line, solve the equation  $x^3 - 3x + 2 = x + 1$  for  $-2 \le x \le 2$ .

(d) By drawing a suitable tangent, find an estimate of the gradient of the curve at the point where x = -1.5.

3 Leo measured the rainfall each day, in millimetres, for 120 days. The cumulative frequency table shows the results.

Rainfall (r mm)	r ≤ 20	r ≤ 25	r ≤ 35	r ≤ 40	r ≤ 60	<i>r</i> ≤ 70
Cumulative frequency	5	13	72	90	117	120

(a) On the grid below, draw a cumulative frequency diagram to show these results.



**(b) (i)** Find the median.

*Answer(b)*(i) ..... mm [1]

(ii) Use your diagram to find the number of days when the rainfall was more than 50 mm.

Answer(b)(ii) ......[2]

(c) Use the information in the cumulative frequency table to complete the frequency table below.

Rainfall (r mm)	$0 < r \le 20$	$20 < r \le 25$	$25 < r \le 35$	$35 < r \le 40$	$40 < r \le 60$	$60 < r \le 70$
Frequency	5		59			3

[2]

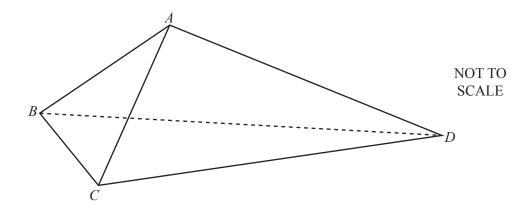
(d) Use your frequency table to calculate an estimate of the mean. You must show all your working.

Answer(d)	mm	[4]
-----------	----	-----

(e) In a histogram drawn to show the information in the table in **part** (c), the frequency density for the interval  $25 < r \le 35$  is 5.9.

Calculate the frequency density for the intervals  $20 < r \le 25$  ,  $40 < r \le 60$  and  $60 < r \le 70$  .

4



The diagram shows a tent ABCD.

The front of the tent is an isosceles triangle ABC, with AB = AC.

The sides of the tent are congruent triangles ABD and ACD.

(a) BC = 1.2 m and angle  $ABC = 68^{\circ}$ .

Find AC.

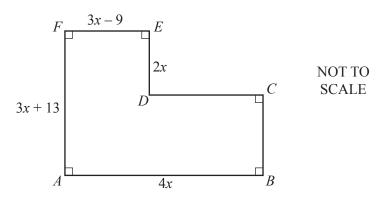
**(b)**  $CD = 2.3 \,\text{m} \text{ and } AD = 1.9 \,\text{m}.$ 

Find angle ADC.

$$Answer(b)$$
 Angle  $ADC = ...$  [4]

(c)	The floor of the tent, triangle $BCD$ , is also an isosceles triangle with $BD = CD$ .
	Calculate the area of the floor of the tent.
	Answer(c)
(d)	When the tent is on horizontal ground, $A$ is a vertical distance 1.25 m above the ground.
	Calculate the angle between AD and the ground.
	Answer(d)

5 (a) The area of shape *ABCDEF* is 24 cm<sup>2</sup>. All lengths are in centimetres.



(i) Show that  $5x^2 + 17x - 12 = 0$ .

Answer(a)(i)

[3]

(ii) Solve, by factorising, the equation  $5x^2 + 17x - 12 = 0$ . You must show all your working.

© UCLES 2015

<b>(b)</b>	Solve the simultaneous equations.
	You must show all your working.

your working. 
$$3x - 2y = 23$$
$$-4x - y = -5$$

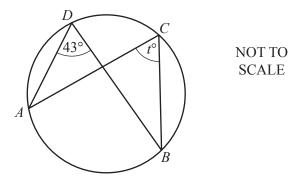
Answer(b) 
$$x = \dots$$
 [3]

(c) Solve the equation.

$$\frac{2(t+3)}{t} - \frac{t}{t+3} = 1$$

$$Answer(c) t = \dots [5]$$

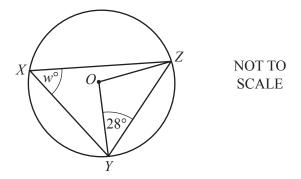
6 (a) (i) A, B, C and D lie on the circumference of the circle.



Find the value of *t*.

$Answer(a)(i) t = \dots$	1	ı	
21165 W CI (W/(1) U			

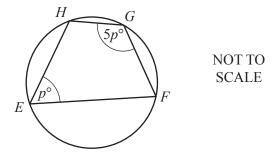
(ii) X, Y and Z lie on the circumference of the circle, centre O.



Find the value of w, giving reasons for your answer.

Answer(a)	)(11) v	v = .	 • • • • • • •	 	 . be	cause	€	 	 		 	 	
		• • • • • • •	 •	 • • • • • • •	 • • • • • •	• • • • • • • • • • • • • • • • • • • •	• • • • • • •	 	 	• • • • • • •	 	 •	
			 	 	 			 	 		 	 . [3	3

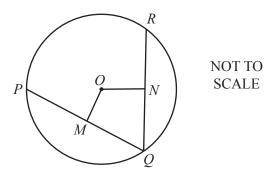
(iii) E, F, G and H lie on the circumference of the circle.



Find the value of *p*, giving a reason for your answer.

Answer(a)(iii) p =	because	2	
		[3	[

**(b)** 



The diagram shows a circle, centre *O*. *PQ* and *QR* are chords.

*OM* is the perpendicular from *O* to *PQ*.

(i) Complete the statement.

$$PM: PQ = \dots$$
 [1]

(ii) ON is the perpendicular from O to QR and PQ = QR.

Complete the statements to show that triangle *OMQ* is congruent to triangle *ONQ*.

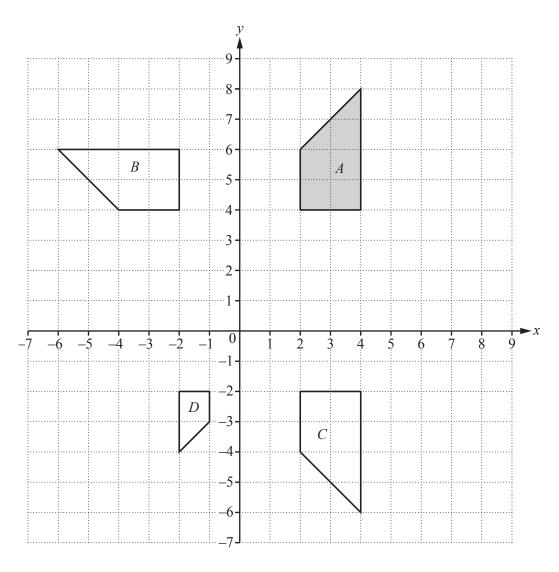
..... is a common side.

..... because M is the midpoint of PQ and N is the midpoint of RQ.

because equal chords are equidistant from ......

[4]

7



- (a) Describe fully the **single** transformation that maps
  - (i) shape A onto shape B,

Answer(a)(i)		
	Г	. 2

(ii) shape A onto shape C,

Answer(a)(ii)	
	ΓΔ.
	1 ′ )

(iii) shape A onto shape D.

1	h)	Find the $2 \times 2$ r	natriv that renr	esents the trans	formation in	nart (a)(iii)
ı	W.	) Find the Z ^ Z i	nauix mai iepi	esems me mans	101111ation ill	part (a)(III).

	/	\
Answer(b)		[2]

- (c) On the grid, draw the image of shape A after a translation by the vector  $\begin{pmatrix} 2 \\ -3 \end{pmatrix}$ . [2]
- (d) Describe fully the **single** transformation represented by the matrix  $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$ .

  Answer(d)

......[2

A li	ne $AB$ joins the points $A$ (3, 4) and $B$ (5, 8).
(a)	Write down the co-ordinates of the midpoint of the line $AB$ .
(b)	Answer(a) ( ) [2] Calculate the distance AB.
(c)	$Answer(b) \ AB =$
(d)	Answer(c)
	$Answer(d) r = \dots [3]$

15 9 f(x) = 2x + 5 $g(x) = 2^x$ h(x) = 7 - 3x(a) Find (i) f(3), *Answer(a)*(i) ......[1] (ii) gg(3). Answer(a)(ii) ..... [2] **(b)** Find  $f^{-1}(x)$ . Answer(b)  $f^{-1}(x) = ....$  [2] (c) Find fh(x), giving your answer in its simplest form.

*Answer(c)* ..... [2]

(d) Find the integer values of x which satisfy this inequality.

$$1 < f(x) \le 9$$

Answer(d) ......[3]

10 The table shows the first five terms of sequences A, B and C.

Sequence	1st term	2nd term	3rd term	4th term	5th term	6th term
A	3	4	5	6	7	
В	0	1	4	9	16	
С	-3	-3	-1	3	9	

(a) Complete the table for the 6th term of each sequer
--

[2]

**(b)** Write down the *n*th term of sequence A.

<i>Answer(b)</i>	1	Ī	l			
------------------	---	---	---	--	--	--

(c) (i) Find the *n*th term of sequence B.

(ii) Find the value of n when the nth term of sequence B is 8281.

$$Answer(c)(ii) \quad n = \dots$$
 [2]

(d) (i) Find the *n*th term of sequence C in its simplest form.

(ii) Find the 8th term of sequence C.

(e) The *n*th term of another sequence D is  $\left(-\frac{1}{2}\right)^{n-1}$ .

Complete the table for the first four terms of sequence D.

Sequence	1st term	2nd term	3rd term	4th term
D				

[3]

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge International Examinations Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cie.org.uk after the live examination series.

Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.